

is said 'intercept' of the regression model and β is called the slope i.e.,

$$\beta = \frac{\partial Y_t}{\partial X_t} \left[\text{Effect upon } Y_t \text{ in response to the change in } X_t \text{ which other variables are remaining unchanged} \right]$$

BASIC ASSUMPTIONS OF THE TWO-VARIABLE LRM

OR

BASIC ASSUMPTIONS OF THE LEAST SQUARE ESTIMATES

Before estimating the parameters involved in the model LRM, we are to take into account some assumptions — some

of them refer to the distribution of random variable, some refer to the relationship between random variables u_t and explanatory variables and some refer to the relationship between explanatory variables themselves. We will group these assumptions into two broad categories -

- (i) Stochastic assumptions
- (ii) other assumptions.

The stochastic assumptions are related to the characteristics of the distribution of random variable.

ASSUMPTIONS:

Following are the main assumptions of the least square estimates of the LRM.

- ① u_t is a real random variable.

This means that the value which u_t may assume in any one period depends on chance.

- ② The mean value of u_t in any particular period is zero i.e., $E(u_t) = 0 \forall t$.

This means that for each value of x_t , u_t may assume various values - some may be greater than zero, some be smaller than zero, but if we consider all the possible values of u_t for any given value

of X_t . This would have an average value equal to zero.

③ The variance of u_t is constant in every period i.e., $\text{Var}(u_t) = E(u_t^2) = \sigma_u^2 \forall t$.

This means

that for all values of X_t , u_t 's will show the same dispersion around their mean.

④ The variable u_t has a normal distribution:

This means that u_t is normally and independently distributed with zero mean and constant variance, σ_u^2 i.e.,

$$u_t \sim N(0, \sigma_u^2)$$

⑤ The explanatory variables are non-stochastic and fixed in the hypothetical process of repeated sampling:

It means that X_t 's are a set of fixed values in the hypothetical process of repeated sampling.

⑥ The random terms of different observations ($u_t, u_{t'}$) are independent. This means that all the covariances of u_t with any $u_{t'}$ are equal to zero. i.e.,

$$\text{Cov}(u_t, u_{t'}) = E(u_t u_{t'}) = 0 \quad \forall t \neq t'$$

$$\begin{aligned} \text{Cov}(u_t, u_t) &= E\left[\{u_t - E(u_t)\} \{u_t - E(u_t)\}\right] \\ &= E\left[\{u_t - 0\} \{u_t - 0\}\right] \\ &= E(u_t^2) \end{aligned}$$

$$\begin{aligned} \text{Cov}(x, x) &= E\left[\{x - E(x)\} \{x - E(x)\}\right] \\ &= E\left[x^2 - xE(x) - E(x)x + \{E(x)\}^2\right] \\ &= E\left[x^2 - 2E(x)x + \{E(x)\}^2\right] \\ &= E(x^2) - 2E(x)E(x) + \{E(x)\}^2 \\ &= E(x^2) - 2\{E(x)\}^2 + \{E(x)\}^2 \\ &= E(x^2) - \{E(x)\}^2 \\ &= \text{Var}(x) \end{aligned}$$

⑦ The explanatory variables are uncorrelated with random disturbance term.

i.e., $\text{Cov}(x_t, u_t) = 0 \quad \forall t$